

ETC

**END SEM EXAMINATION (SPRING 2013)**

**Information Theory and Statistics (RSSP)**

Marks: 50

Max. time: 3 hrs.

**General instructions:**

- 1. Please attempt questions in the same order as they appear in the paper
- 2. Explain answers with clarity using Logic and Maths, credit is for method and not final answer

**Q1.**

a) A spy-system(CDMA) is to be designed for information communication. Develop & justify the conditions applying on  $p$  and  $H(p)$  ? {Max Entropy/Cover} 5

b) Observers A and B conclude with statistical surveys giving  $p$  and  $q$  as distributions of data. Justify that the decision error is upper bounded by

$P(\text{error}) \leq \exp[-D(p||q) * n * H(p)]$  {Universal Source coding/Chernoff} 5

**Q2.**

a) Depicting a Universal Trellis by Binary Tree, prove the Kraft-McMillan Inequality. What is achieved by this rule? {Prefix free coding/Karush} 5

b) What are main constraints in design of: Sampling, Quantization; for a noiseless source? {Representation/Shannon} 5

c) Develop the major blocks (architecture) and steps (algorithm) in a Vector Quantizer for Image Compression. {Maths of Quantization/Gray} 5

**Q3.**

a) Given letters 1,2,3,4,5,6 are outcomes of a sample space (assume equi-probable or, non-uniform distribution). Design Dictionary/Codebook for the following cases:

- i) not uniquely decode-able
- ii) prefix free
- iii) uniquely decodable {Codebook generation/Cover} 5

b) Reason why a Uniform Length Source Coding is not an optimal choice for representation. {Equiprobable randomness/Ziv-Briemann} 5

c) Use Linear Programming or otherwise prove that  $H_2(p)$  indeed is minimum length description of a universal program with Binary states. Can this be generalized for  $H_a(p)$ .

{Complexity theory/Kolmogorov-Chaitin} 5

**Q4.**

a) Depict with 2-state Markov process a model for information processing. {Information coding and transmission/Verdu} 5

b) Errors occur in typing from a keypad with alphanumeric letters. Errors arise due to the four neighbourhood keys around any given key. Assume a keypad and formulate the maximum rate of typing for reliability (error free typing)? {Information capacity/Shannon} 5

**OR**

c) Develop Shannon's Information model and measure for Reliable communication {Digital Information/Shannon} 5

