

**COLLEGE OF ENGINEERING, PUNE**  
(An Autonomous Institute of Government of Maharashtra)

**End Semester Examination**

**(DE - 09024) Signals and Systems**

**Programme: T. Y. B. Tech (Instrumentation and Control)**

Year: 2013-14  
Duration: 3 hrs

Semester: I  
Max. Marks: 60

**Instructions:**

1. Solve any **THREE** questions.
  2. Assume suitable data if necessary.
  3. Figures to right indicate full marks.
  4. Draw neat figures wherever required.
  5. Use of non-programmable calculator is allowed.
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Q.1 Answer the following:

A) Determine whether the following system is linear, stable, causal and time-invariant using appropriate tests:

$$y(n) = nx(n) + x(n+2) + y(n-2)$$

[8]

B) What is FFT? Draw and explain in detail Decimation in frequency (DIF) FFT algorithm for 8 point data.

[8]

C) Choose appropriate choice(s):

[4]

1. What is the condition for perfect reconstruction of an analog signal from its Discrete signal?

- a. the signal should be band limited
- b. the signal should have all frequency components
- c. signal should contain high frequency
- d. none

2. If  $x(n) = \{\dots -2, -4, 2, 0, 5, 7, \dots\}$ . Then

↑

what is the value of  $x(2)$ ?

- a) -2
- b) -4
- c) 0
- d) 5

3. What are the specifications that are needed to completely describe a filter?

- a) pass band ripple, stop band ripple,  $W_s$ ,  $W_p$
- b) pass band ripple, stop band ripple,  $W_p$  only
- c) pass band ripple, stop band ripple
- d)  $W_s$ ,  $W_p$

4. The signal which exists only at  $t=0$ , whose area is unity referred as continuous

time unit

a) Impulse

c) Series

b) Time

d) Level

Q. 2 Answer the following:

A) Obtain the convolution of the following sequences:

$$x_1(n) = (1, 2, \underset{\uparrow}{1}, 2, 1)$$

$$x_2(n) = (0, 1, 2)$$

Use graphical approach. [6]

B) Find inverse discrete Fourier transform the following:

$$X(k) = (2, 2 + 2j, -2, 2 - 2j)$$
 [8]

C) The input and the output of a causal LTI system are related by the differential equation.

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 6y(t) = x(t)$$

a) Find the impulse response of the system.

b) What is the impulse response of the system if  $x(t) = te^{-4t}u(t)$  [6]

Q. 3 Answer the following:

A) What is sampling theorem? How is it important in signal processing? Elaborate with proper illustration. [4]

B) Find the inverse Z transform of

$$X(z) = \frac{3z^{-1}}{(1-z^{-1})(1-2z^{-1})}$$

a) If ROC;  $|z| > 2$ b) If ROC;  $|z| < 1$ c) If ROC;  $1 < |z| < 2$  [6]

C) Choose appropriate choice(s): [5]

1. For the analog signal given below

$$m(t) = 4 \cos 100\pi t, \text{ then the value of } F_s \text{ is}$$

a) 1000 Hz

b) 10 KHz

c) 100 Hz

d) 10000 Hz

2. Z transform of sequence  $x[n] = \{ 8, 7, 2, 0, 0, -5 \}$  where  $x[0] = 2$ , is

a)  $8Z^2 + 7Z + 2 - 5Z^{-3}$

b)  $8Z^{-2} + 7Z^{-1} + 2 - 5Z^3$

c)  $8Z^2 + 7Z + 2 - 5Z^{-1}$

3. What is the condition for linearity?

- a)  $T[a_1 * x_1(n) + a_2 * x_2(n)]$   
 $= a_1 * T[x_1(n)] + a_2 * T[x_2(n)]$
- b)  $T[a_1 * x_1(n) + a_2 * x_2(n)] = x_1(n) + x_2(n)$
- c)  $T[a_1 * x_1(n) + a_2 * x_2(n)]$   
 $= T[x_1(n)] + T[x_2(n)]$
- d)  $T[a_1 * x_1(n) + a_2 * x_2(n)]$   
 $= T[a_1 * x_1(n)] + T[a_2 * x_2(n)]$

4. The sampling theorem was given by \_\_\_\_\_ in 1928.

- a) Shannon  
 b) Nyquist  
 c) Oppenheim  
 d) Schfer

5. For a system to be completely characterized by its impulse response  $h(n)$  it has to be

- a) linear  
 b) stable  
 c) causal  
 d) LTI

D) Consider recursive relation

$$y(n) = 3y(n-1) + y(n-2) + 5x(n) - 2x(n-1)$$

Obtain its non-canonical form and canonical form implementation. [5]

Q. 4 Answer the following:

A) You are required to design and realize audio processing application, suggest a suitable scheme required for realization and explain in detail. [5]

D) Find the Z Transform of the signal

$$x(n) = n \left[ \left( \frac{1}{2} \right)^n u(n) * \left( \frac{1}{3} \right)^n u(n) \right]$$

[6]

B) Compare analog and digital filters [2]

C) Choose appropriate choice(s): [3]

1. If  $X(w) = e^{-jw}$  then what is  $x(n)$ ?

- a.  $\delta(n)$   
 b.  $\delta(n-1)$   
 c.  $\delta(n+1)$   
 d.  $\delta(n+4)$

2. If  $x_1(n) \leftrightarrow X_1(w)$  and  $x_2(n) \leftrightarrow X_2(w)$  then what is the fourier transform of  $[x_1(n)] * [x_2(n)]$ ?

- a.  $X_1(w).X_2(w)$   
 b.  $X_1(w)/X_2(w)$

- c.  $X1(w) + X2(w)$
- d.  $X1(w) - X2(w)$

3. Mathematically discrete time unit impulse can be obtained as

- a)  $\delta[n] = u[n]$
- b)  $\delta[n] = u[n] - u[n-1]$
- c)  $\delta[n] = u[n] + u[n+1]$
- d)  $\delta[n] = u[n] - u[n-2]$

D) Find whether the signal

$$x(t) = \begin{cases} t-2 & -2 \leq t \leq 0 \\ 2-t & 0 \leq t \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

is energy signal or power signal. Also find the energy and power of the signal.

[4]

\*\*\*\*\*All the Best\*\*\*\*\*